Scheduling HVAC loads to promote renewable generation integration with a learning-based joint chance-constrained approach

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Abstract—The integration of distributed renewable generation (DRG) in distribution networks can be effectively promoted by scheduling flexible resources such as heating, ventilation, and air conditioning (HVAC) loads. However, finding the optimal scheduling for them is nontrivial because DRG outputs are highly uncertain. To address this issue, this paper proposes a learning-based joint chance-constrained approach to coordinate HVAC loads with DRG. Unlike cutting-edge works adopting individual chance constraints to manage uncertainties, this paper controls the violation probability of all critical constraints with joint chance constraints (JCCs). This joint manner can explicitly guarantee the operational security of the entire system based on operators' preferences. To overcome the intractability of JCCs, we first prove that JCCs can be safely approximated by robust constraints with proper uncertainty sets. A famous machine learning algorithm, one-class support vector clustering, is then introduced to construct a small enough polyhedron uncertainty set for these robust constraints. A linear robust counterpart is further developed based on the strong duality to ensure computational efficiency. Numerical results based on various distributed uncertainties confirm the advantages of the proposed model in optimality and feasibility.

Index Terms—Demand-side flexibility, joint chance constraints, support vector clustering, HVAC systems, renewable energies NOMENCLATURE

Indices

i	Index of buses.
m	Index of constraints.
n	Index of samples.
t	Index of hours.
Parameters	
C_i	Heat capacity of building i (MWh/°C).

$d_{i,t}$	Heat	load	from	indoor	sources	in	the	buildings
	connected to bus i in hour t (MW).							

COP_i Coefficient of performance of the HVAC system in building i (MW/MW).

- $\overline{G}_{i,t}$ Nominal active power output of distributed renewable generator on bus i in hour t (MW). g_i Heat transfer coefficient between indoor and outdoor
- g_i environments in building *i* (MW/°C).
- $p_{i,t}^{e}, q_{i,t}^{e}$ Active and reactive base loads on bus *i* in hour *t* (MW).
- \overline{p}_i Upper bound of the HVAC's active power in building *i* (MW).
- r_{ij}, x_{ij} Resistance and reactance of branch (i, j) (p.u.).

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S_{ij}^{\max}	Maximum allowable apparent power flow on branch
$\sim ij$	(i, j) (MW).
lpha,eta	Dual variables in problem P-SVC . Note that they are fixed when solving P2 .
ϵ	Risk parameter.
$\epsilon \eta_t^{ m buy}$, $\eta_t^{ m sell}$	Unit price for purchasing and selling electricity (\$/MWh).
$\overline{\theta}_i, \underline{\theta}_i$	Upper and lower bounds of the thermal comfort
<i>•i</i> , <u><i>•</i></u> <i>i</i>	region in building i (°C).
θ_t^{out}	Outdoor temperature at hour t (°C).
ϕ_i	Power factor of the HVAC system in the buildings
T T	connected to bus i
Uncertainti	es
$\xi_{i,t}$	The uncertain level of the active power output of the
	distributed renewable generator on bus i in hour t .
U _t Variables	Uncertainty set.
EC_t	Total cost in hour t (\$).
EC_t G_t	Total cost in hour t (\$). Net active power at the substation in hour t (MW).
G_t	Net active power at the substation in hour t (MW). Center of the minima sphere. Active and reactive power injection on bus i in hour
G_t o $p_{i,t}, q_{i,t}$	Net active power at the substation in hour t (MW). Center of the minima sphere. Active and reactive power injection on bus i in hour t (MW).
G_t o	Net active power at the substation in hour t (MW). Center of the minima sphere. Active and reactive power injection on bus i in hour t (MW). Active and reactive power of the HVAC system in
G_t o $p_{i,t}, q_{i,t}$	Net active power at the substation in hour t (MW). Center of the minima sphere. Active and reactive power injection on bus i in hour t (MW). Active and reactive power of the HVAC system in building i in hour t (MW). Active and reactive power flows on branch (i, j) in
G_t o $p_{i,t}, q_{i,t}$ $p_{i,t}^{HV}, q_{i,t}^{HV}$	Net active power at the substation in hour t (MW). Center of the minima sphere. Active and reactive power injection on bus i in hour t (MW). Active and reactive power of the HVAC system in building i in hour t (MW). Active and reactive power flows on branch (i, j) in hour t (MW). Auxiliary variables for extracting the quadratic con-
$\begin{array}{l} G_t \\ \textbf{o} \\ p_{i,t}, q_{i,t} \\ p_{i,t}^{HV}, q_{i,t}^{HV} \\ P_{ij,t}, Q_{ij,t} \\ P_{ij,t}^{aux}, Q_{ij,t}^{aux} \end{array}$	Net active power at the substation in hour t (MW). Center of the minima sphere. Active and reactive power injection on bus i in hour t (MW). Active and reactive power of the HVAC system in building i in hour t (MW). Active and reactive power flows on branch (i, j) in hour t (MW). Auxiliary variables for extracting the quadratic con- straint from chance constraints.
$\begin{array}{l} G_t \\ \textbf{o} \\ p_{i,t}, q_{i,t} \\ p_{i,t}^{HV}, q_{i,t}^{HV} \\ P_{ij,t}, Q_{ij,t} \\ P_{ij,t}^{aux}, Q_{ij,t}^{aux} \\ R \end{array}$	Net active power at the substation in hour t (MW). Center of the minima sphere. Active and reactive power injection on bus i in hour t (MW). Active and reactive power of the HVAC system in building i in hour t (MW). Active and reactive power flows on branch (i, j) in hour t (MW). Auxiliary variables for extracting the quadratic con- straint from chance constraints. Radius of the minima sphere.
$\begin{array}{l} G_t \\ \textbf{o} \\ p_{i,t}, q_{i,t} \\ p_{i,t}^{HV}, q_{i,t}^{HV} \\ P_{ij,t}, Q_{ij,t} \\ P_{ij,t}, Q_{ij,t}^{aux} \\ P_{ij,t}^{aux}, Q_{ij,t}^{aux} \\ R \\ U_{i,t} \end{array}$	Net active power at the substation in hour t (MW). Center of the minima sphere. Active and reactive power injection on bus i in hour t (MW). Active and reactive power of the HVAC system in building i in hour t (MW). Active and reactive power flows on branch (i, j) in hour t (MW). Active and reactive power flows on branch (i, j) in hour t (MW). Auxiliary variables for extracting the quadratic constraint from chance constraints. Radius of the minima sphere. Voltage of bus i in hour t (p.u.).
$\begin{array}{l} G_t \\ \textbf{o} \\ p_{i,t}, q_{i,t} \\ p_{i,t}^{HV}, q_{i,t}^{HV} \\ P_{ij,t}, Q_{ij,t} \\ P_{ij,t}, Q_{ij,t}^{aux} \\ P_{ij,t}^{aux}, Q_{ij,t}^{aux} \\ R \\ U_{i,t} \end{array}$	Net active power at the substation in hour t (MW). Center of the minima sphere. Active and reactive power injection on bus i in hour t (MW). Active and reactive power of the HVAC system in building i in hour t (MW). Active and reactive power flows on branch (i, j) in hour t (MW). Active and reactive power flows on branch (i, j) in hour t (MW). Auxiliary variables for extracting the quadratic constraint from chance constraints. Radius of the minima sphere. Voltage of bus i in hour t (p.u.). Generic decision variable.
$\begin{array}{l} G_t \\ \textbf{o} \\ p_{i,t}, q_{i,t} \\ p_{i,t}^{HV}, q_{i,t}^{HV} \\ P_{ij,t}, Q_{ij,t} \\ P_{ij,t}^{aux}, Q_{ij,t}^{aux} \\ R \end{array}$	Net active power at the substation in hour t (MW). Center of the minima sphere. Active and reactive power injection on bus i in hour t (MW). Active and reactive power of the HVAC system in building i in hour t (MW). Active and reactive power flows on branch (i, j) in hour t (MW). Active and reactive power flows on branch (i, j) in hour t (MW). Auxiliary variables for extracting the quadratic constraint from chance constraints. Radius of the minima sphere. Voltage of bus i in hour t (p.u.).

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I. INTRODUCTION

THE increasing penetration of renewable generation mitigates the demand for fossil energy. However, it also exacerbates the imbalance between demands and generation due to the stochastic characteristics of renewable generation [1]. As a result, much distributed renewable generation (DRG) has to be curtailed to maintain operational security. Fortunately, the integration of DRG can be promoted by properly scheduling flexible sources in distribution networks [2]. Due to the natural ability of buildings to store heating/cooling power, heating, ventilation, and air conditioning (HVAC) loads can be regarded as desirable demand-side flexible sources [3], [4]. Hence, tons of scheduling methods have been proposed to realize the proper coordination between HVAC loads and DRG. For instance, reference [5] proposed an aggregation method to identify the operational flexibility of multiple buildings. Reference [6] developed a simplification method to model the flexibility of large-scale HVAC systems. Reference [7] regarded HVAC loads as virtual battery systems and provided a control scheme to unlock their flexibility.

However, it is hard to predict DRG outputs perfectly due to their stochastic characteristics. Thus, uncertainties from forecasting errors of DRG must be considered during the power scheduling to avoid constraint violations [8]. Robust optimization has traditionally been used to manage these uncertainties [9]. However, it is usually overly conservative because every constraint should be satisfied with all possible realizations of uncertainties. Chance-constrained programming (CCP) is an alternative method to manage the uncertainties from DG in OPF [10]. It allows constraint violations with a small probability so that operators can effectively balance robustness and optimality based on their preferences. Reference [11] proposed a CCP-based framework to coordinate thermostatically controlled loads with uncertain DRG. Reference [12] leveraged CCP to handle the uncertainties from DRG during the planning of integrated energy systems. Reference [13] developed a multi-period CCP framework to aggregate HVAC loads for reserve services. Reference [14] utilized a distributionally robust CCP method to schedule flexible loads and energy storage systems in distribution networks. Reference [15] proposed a fast distributionally robust CCP framework to utilize the load flexibility of HVAC loads for cost minimization. However, most CCP-based methods, including [12]–[15], control the violation probability of critical constraints individually. For a distribution system, violations of any constraint may affect operational safety. Therefore, system security is hard to guarantee for this individual manner because it does not restrict all critical constraints to be satisfied simultaneously with a predetermined probability [16]. For example, suppose a system has two security constraints, i.e., $a_1 \in \mathcal{A}_1$ and $a_2 \in \mathcal{A}_2$. Now we wish to maintain its system security with a probability of $1 - \epsilon$, i.e., $\mathbb{P}((a_1 \notin \mathcal{A}_1) \lor (a_2 \notin \mathcal{A}_2)) \leq \epsilon$. If we individually describe the probability satisfaction of the two security constraints, i.e., $\mathbb{P}(a_1 \notin \mathcal{A}_1) \leq \epsilon$ and $\mathbb{P}(a_2 \notin \mathcal{A}_2) \leq \epsilon$, then the corresponding violation probability is $\mathbb{P}((a_1 \notin \mathcal{A}_1) \lor (a_2 \notin \mathcal{A}_2))$ = $\mathbb{P}\left(a_1 \notin \mathcal{A}_1\right) + \mathbb{P}\left(a_2 \notin \mathcal{A}_2\right) - \mathbb{P}\left(\left(a_1 \notin \mathcal{A}_1\right) \land \left(a_2 \notin \mathcal{A}_2\right)\right) \leq$ $2\epsilon - \mathbb{P}((a_1 \notin \mathcal{A}_1) \land (a_2 \notin \mathcal{A}_2))$. Since the term $2\epsilon -$ $\mathbb{P}((a_1 \notin \mathcal{A}_1) \land (a_2 \notin \mathcal{A}_2)) \geq 2\epsilon - \mathbb{P}(a_1 \notin \mathcal{A}_1) \geq \epsilon$, this individual manner may not be able to ensure the system security with the pre-determined probability (i.e. $1 - \epsilon$).

The violation probabilities of critical constraints should be jointly considered due to the security concern of power systems [17], [18]. Therefore, joint chance constraints (JCCs), which jointly describe these probabilities, are preferable for coordinating HVAC systems with DRG in distribution networks. Unfortunately, JCCs are much more intractable than individual ones [19]. Hence, much effort has been made to overcome this. Generally speaking, the published methods for handling JCCs can be divided into three categories.

1) Bonferroni approximation: The Bonferroni approximation leverages multiple individual chance constraints (ICCs) to approximate an intractable JCC. For instance, reference [20] employed the Bonferroni approximation to handle the JCCs in operating drinking water networks. References [21], [22] provided tighter upper bounds for the Bonferroni approximation to improve its optimality. However, it requires that the summation of all individual violation probabilities is no larger than the joint one to guarantee the feasibility of solutions [10]. Hence, some individual violation probabilities may be very small. In this case, the Bonferroni approximation may derive overly conservative solutions [17].

2) Scenario approach: The scenario approach approximates JCCs by requiring constraints to be robust for a finite number of scenarios. With a sufficient number of scenarios, the feasibility of the original JCC can be guaranteed [10]. Reference [23] utilized the scenario approach to approximate JCCs with scenario-wise deterministic scenarios. References [24], [25] designed box uncertainty sets to cover all scenarios and proposed a robust optimization-based inner approximation to reduce computational burdens. Other types of uncertainty sets, e.g., ellipsoids [26] or convex hulls [27], have also been combined with the scenario approach to improve optimality. However, the approach may still be overly conservative once some extreme samples of uncertainties are chosen as scenarios.

3) Sample average approximation: The sample average approximation (SAA) utilizes enough empirical samples to approximate the underlying true distribution of uncertainties. SAA introduces auxiliary binary variables to identify safe samples (satisfying all constraints) and unsafe samples (causing constraint violations). By restricting the total number of unsafe samples, JCCs can be approximated by sample-wise deterministic constraints. Note that SAA differs from the scenario approach by accepting small constraint violations. Hence SAA can potentially achieve better optimality [10]. SAA has been utilized to handle JCCs in power grid planning [28] and unit commitment [29]. However, since SAA needs to introduce many binary variables, it is computationally expensive.

This paper aims to design an energy- and time-efficient scheduling method to overcome the challenges above, i.e., overly conservative results or huge computational burdens. To achieve this goal, a novel scheduling approach is proposed. Its main contributions are threefold:

- We propose a joint chance-constrained model to manage the uncertainties from DRG during the coordination of HVAC loads and DRG in distribution networks. The violation probabilities of all critical constraints are jointly considered so that the system security can be explicitly guaranteed with a high probability.
- 2) We design a robust approximation with a novel learningbased uncertainty set to replace intractable JCCs. By leveraging the one-class support vector clustering (OC-SVC) algorithm, we establish a small polyhedron uncertainty set to tightly cover most historical samples for an energy-efficient solution. We further prove that this uncertainty set can guarantee the feasibility of solutions. To the best of our knowledge, this is the first adoption of the OC-SVC-based uncertainty set for joint chanceconstrained scheduling problems.
- We develop a tractable robust counterpart for the OC-SVC-based uncertainty set. This counterpart is linear and can be easily solved by off-the-shelf solvers with guaranteed computational efficiency.

The rest of this paper is organized as follows. Section II provides the system model. Section III presents the procedure of the proposed model. Section IV discusses simulation results, and section V presents the conclusion.

II. PROBLEM FORMULATION

HVAC systems and DRG are usually connected to distribution networks. By properly designing the power schedule of HVAC systems, the integration of uncertain DRG can be promoted to reduce the total cost of distribution networks. Indoor thermal discomfort should be avoided to guarantee the service quality of HVAC systems. The scheduling strategy should satisfy bus voltage and branch power flow limitations to ensure the system's operational security.

A. Modeling of building thermal dynamics

The indoor temperature variation in buildings can be described by a widely-used energy conservation model,

$$\theta_{i,t}^{\text{in}} = a_i^{\text{in}} \theta_{i,t-1}^{\text{in}} + a_i^{\text{out}} \theta_{t-1}^{\text{out}} + a_i^{\text{h}} d_{i,t-1} + a_i^{\text{q}} p_{i,t-1}^{\text{HV}}, \quad \forall i \in \mathcal{I}, \quad \forall t \in \mathcal{T},$$
(1)

where $\theta_{i,t}$ and $\theta_{t-1}^{\text{out}}$ are the respective temperatures of the indoor and outdoor environments; $d_{i,t}$ is the heat load contributed by indoor sources (e.g., humans and electric devices); $p_{i,t}^{\text{HV}}$ is the active power of the HVAC system; and

$$\begin{cases} a_i^{\text{in}} = e^{-\frac{g_i \Delta t}{C_i}}, & a_i^{\text{out}} = 1 - a_i^{\text{in}}, \\ a_i^{\text{h}} = \frac{1}{g_i} \cdot a_i^{\text{out}}, & a_i^{\text{q}} = -\text{COP}_i \cdot a_i^{\text{h}}, \end{cases} \quad \forall i \in \mathcal{I}, \qquad (2)$$

where C_i is the heat capacity of the building connected to the *i*-th node, g_i is the corresponding heat transfer coefficient between indoor and outdoor environments, and Δt is the length of the optimization time interval; COP_i is the coefficient of performance of the HVAC system. The reactive power of the HVAC system calculated by

$$q_{i,t}^{\mathrm{HV}} = \sqrt{(1-\phi_i^2)} / \phi_i \cdot p_{i,t}^{\mathrm{HV}}, \ \forall i \in \mathcal{I}, \forall t \in \mathcal{T},$$
(3)

where ϕ_i is the power factor of the *i*-th HVAC system. Due to thermal comfort requirements and device limitations, the indoor temperature and active power of HVAC systems are bounded by

$$\underline{\boldsymbol{\theta}} \leq \boldsymbol{\theta}_t^{\text{in}} \leq \overline{\boldsymbol{\theta}}, \quad \boldsymbol{p}_t^{\text{HV}} \leq \overline{\boldsymbol{p}}, \quad \forall t \in \mathcal{T},$$
(4)

where $\underline{\theta}$ and $\overline{\theta}$ are the lower and upper bounds, respectively, of the comfortable range; \overline{p} is the upper limitation of the active power of HVAC systems.

B. Modeling of distribution networks

1) Operation cost: The energy cost of a distribution network is the cost of purchasing electricity (the net power at the substation is positive) plus the profit from selling power to the upper-level grid (net power is negative),

$$EC_t = (\eta^{\text{buy}} G_t^{\text{buy}} - \eta^{\text{sell}} G_t^{\text{sell}}) \Delta t, \quad \forall t \in \mathcal{T},$$
(5)

$$G_t^{\text{buy}} - G_t^{\text{sell}} = G_t^{\text{g}}, \quad G_t^{\text{buy}} \ge 0, \quad G_t^{\text{sell}} \ge 0, \quad \forall t \in \mathcal{T}.$$
 (6)

where EC_t is the energy cost at time $t \in \mathcal{T}$; η^{buy} and η^{sell} are the per-unit prices of electricity purchasing and selling, respectively, G_t^{buy} and G_t^{sell} are two auxiliary variables; G_t^g is the net power at the substation; Δt is the length of a time slot.

2) *Nodal power injections:* The nodal power injections can be expressed as¹

$$\boldsymbol{p}_t = -\boldsymbol{p}_t^{\text{HV}} - \boldsymbol{p}_t^{\text{e}} + \boldsymbol{G}_t^{\text{DG}} * \boldsymbol{\lambda}_t, \ 0 \le \boldsymbol{\lambda}_t \le 1, \ \forall t \in \mathcal{T}, \quad (7)$$

$$\boldsymbol{q}_t = -\boldsymbol{q}_t^{\mathrm{HV}} - \boldsymbol{q}_t^{\mathrm{e}}, \quad \forall t \in \mathcal{T},$$
(8)

where p_t^{HV} and q_t^{HV} are vector forms of $p_{i,t}^{\text{HV}}$ and $q_{i,t}^{\text{HV}}$, respectively; G_t^{DG} and λ_t are the available output and utilization rate of DRG, respectively; p_t^e and q_t^e are the active and reactive base loads, respectively (i.e., the loads apart from the power demands of HVAC systems); "*" denotes element-wise multiplication. In practice, the available output of DRG is usually uncertain, which can be expressed as

$$\boldsymbol{G}_{t}^{\mathrm{DG}} = \overline{\boldsymbol{G}}_{t}^{\mathrm{DG}} * (1 + \boldsymbol{\xi}_{t}), \quad \forall t \in \mathcal{T},$$
(9)

where $\overline{G}_t^{\text{DG}}$ and ξ_t are the nominal available power and uncertain level of DRG, respectively.

3) Power flow constraints: Buildings with flexible HVAC loads are spatially distributed, so the coordination strategy should satisfy power flow constraints, i.e., bus voltage and branch power flow limitations. The power flow in a distribution network can be described by the linearized DistFlow [30]:²

$$\begin{cases}
P_{ij,t} = \sum_{k \in \mathcal{C}_j} P_{jk,t} - p_{j,t}, \\
Q_{ij,t} = \sum_{k \in \mathcal{C}_j} Q_{jk,t} - q_{j,t}, \\
U_{j,t} = U_{i,t} - 2(r_{ij}P_{ij,t} + x_{ij}Q_{ij,t}), \\
\forall (i,j) \in \mathcal{B}, \ \forall t \in \mathcal{T},
\end{cases}$$
(10)

where $P_{ij,t}$ and $Q_{ij,t}$ are the active and reactive power flows, respectively, on branch $(i, j) \in \mathcal{B}$; *i* and *j* are the bus indexes, $i, j \in \mathcal{I}$; $p_{j,t}$ and $q_{j,t}$ are the active and reactive power injections, respectively, at bus *j*; U_i is the square of the voltage at bus *i*; r_{ij} and x_{ij} are the resistance and reactance, respectively, of branch (i, j); and set \mathcal{C}_j contains the child bus indexes of bus *j*, $\mathcal{C}_j \subseteq \mathcal{I}$. The net power at substation G_t^g is the summation of the active power flows from the slack bus (i = 0) to its child buses, as follows

$$G_t^{\mathsf{g}} = \sum_{j \in \mathcal{C}_0} P_{0j,t}, \quad \forall t \in \mathcal{T}.$$
 (11)

All bus voltages and branch power flows should lie in a proper range to ensure system security. According to (7) and (8), uncertainty ξ_t affects the power injections on each bus. Based on the linearized Distflow (10), this uncertainty further propagates to the square of the bus voltage U_t , and branch power flows P_t and Q_t . To maintain system security, a JCC

¹While we assume DRG only outputs active power here, the proposed model can be readily extended to consider a DG's reactive power output.

²The linearized DistFlow model is an approximation of power flow equations, so it may introduce approximation errors. Nevertheless, reference [31] pointed out that this approximation error is usually small and will not affect the results significantly (e.g., if the maximum allowable voltage deviation is 5%, then the maximum relative error is only 0.25%).

is employed to manage the uncertainties:

$$\mathbb{P}\left(\begin{array}{c} U_{i,\min} \leq U_{i,t} \leq U_{i,\max}, \ \forall i \in \mathcal{I}, \\ P_{ij,t}^2 + Q_{ij,t}^2 \leq (S_{ij}^{\max})^2, \forall (i,j) \in \mathcal{B}, \end{array}\right) \geq 1 - \epsilon, \quad (12)$$

where $U_{i,\min}$ and $U_{i,\max}$ are the lower and upper bounds of the bus voltage; S_{ij}^{\max} is the maximum allowable apparent power flow. Symbol ϵ is the risk parameter, which defines the maximum allowable probability of constraint violations.

Remark 1. Here, we use JCCs instead of individual ones to control the violation probability of all security constraints under the impacts of uncertainties from DRG. This is preferable in the coordination of DRG and HVAC loads because it can accurately ensure the security of the entire system with a predetermined confidence level.

4) Linearization of the quadratic JCC: There are quadratic constraints inside the probability operator of (12), which are intractable. To address this issue, we introduce auxiliary variables $P_{ij,t}^{aux}$ and $Q_{ij,t}^{aux}$, and conservatively approximate each quadratic constraint inside the probability operator by

$$\begin{cases} (P_{ij,t}^{aux})^2 + (Q_{ij,t}^{aux})^2 \le (S_{ij}^{max})^2, \\ |P_{ij,t}| \le P_{ij,t}^{aux}, \ |Q_{ij,t}| \le Q_{ij,t}^{aux}. \end{cases} \quad \forall (i,j) \in \mathcal{B}.$$
(13)

Note that $P_{ij,t}^{aux}$ and $Q_{ij,t}^{aux}$ are deterministic. Thus, the conic constraint, i.e., the first line of (13), does not contain any uncertainty. Then, by substituting (13), the quadratic JCC (12) can be approximated by a deterministic second-order cone constraint plus a linear JCC

$$(P_{ij,t}^{aux})^{2} + (Q_{ij,t}^{aux})^{2} \leq (S_{ij}^{max})^{2}, \quad \forall (i,j) \in \mathcal{B},$$

$$\mathbb{P} \begin{pmatrix} U_{i,\min} \leq U_{i,t} \leq U_{i,\max}, \forall i \in \mathcal{I}, \\ |P_{ij,t}| \leq P_{ij,t}^{aux}, |Q_{ij,t}| \leq Q_{ij,t}^{aux}, \forall (i,j) \in \mathcal{B}, \end{pmatrix}$$

$$\geq 1 - \epsilon, \forall t \in \mathcal{T}.$$
(15)

Obviously, any feasible solution of (15) must be feasible for (12). Hence (15) can guarantee the feasibility of solutions.

C. Optimization problem

Our goal is to minimize the total cost. Thus, the optimization problem is formulated as

$$\min_{\substack{(\boldsymbol{p}_t^{\mathsf{HV}}, \boldsymbol{\lambda}_t, \boldsymbol{P}_t^{\mathsf{aux}}, \boldsymbol{Q}_t^{\mathsf{aux}}) \forall t \in \mathcal{T}}} \mathbb{E}\left(\sum_{t \in \mathcal{T}} EC_t\right), \quad (\mathbf{P1})$$

s.t. Eqs. (1)-(11) and (14)-(15).

III. LEARNING-BASED REFORMULATION FOR JOINT CHANCE CONSTRAINTS

Constraint (15) is intractable because of the inside probability operator. We address this issue through a learning-based approach. We first propose a robust approximation for the JCC to eliminate the intractable probability operator. Then, an OC-SVC-based method is employed to construct a tight polyhedron uncertainty set for the previous robust approximation. A linear counterpart for the proposed OC-SVC-based uncertainty set is further developed to ensure computational tractability.

A. Robust approximation of the JCC

Observing that all constraints inside the probability operator of (15) are linear, they can be expressed in a generic form

$$(\boldsymbol{H}_{m,t}\boldsymbol{\xi}_t)^{\mathsf{T}}\boldsymbol{y}_t \leq b_{m,t}(\boldsymbol{y}_t), \forall m \in \mathcal{M}, \forall t \in \mathcal{T},$$
(16)

where $H_{m,t}$ and ξ_t are the coefficient matrix and random variable, respectively, in each constraint; $y_t = [p_t^{\text{HV}}, \lambda_t, P_t^{\text{aux}}, Q_t^{\text{aux}}]$ is the decision variable vector; $b_{m,t}$ is an affine function of y_t ; and $m \in \mathcal{M} = \{1, 2, \dots, M\}$ is the index of the constraints inside the probability operator. By defining a new function $f_t(y_t, \xi_t)$ as

$$f_t(\boldsymbol{y}_t, \boldsymbol{\xi}_t) = \max_{m \in \mathcal{M}} \left((\boldsymbol{H}_{m,t} \boldsymbol{\xi}_t)^{\mathsf{T}} \boldsymbol{y}_t - b_{m,t}(\boldsymbol{y}_t) \right), \forall t \in \mathcal{T}, \quad (17)$$

Eq. (15) can be expressed as

$$\mathbb{P}\left(f_t(\boldsymbol{y}_t, \boldsymbol{\xi}_t) \le 0\right) \ge 1 - \epsilon, \quad \forall t \in \mathcal{T}.$$
(18)

If we can find an uncertainty set \mathcal{U}_t satisfying

$$\mathbb{P}\left(\boldsymbol{\xi}_t \in \mathcal{U}_t\right) \ge 1 - \epsilon, \forall t \in \mathcal{T},\tag{19}$$

the intractable JCC (18) can be approximately expressed by a robust constraint,

$$\max_{\boldsymbol{\xi}_t \in \mathcal{U}_t} \left(f_t(\boldsymbol{y}_t, \boldsymbol{\xi}_t) \right) \le 0, \forall t \in \mathcal{T},$$
(20)

and the probability operator can be eliminated. Obviously, the key problem of this robust approximation is to find an appropriate U_t , which should satisfy feasibility, optimality, and tractability requirements:

- 1) Feasibility: U_t must cover at least $100(1 \epsilon)\%$ of samples in the historical dataset, i.e., Eq. (19);
- 2) **Optimality**: The space covered by U_t should be small, so that the obtained solution can achieve desirable energy efficiency;
- 3) **Tractability**: The robust approximation (20) with U_t as its uncertainty set must have a tractable counterpart so that it can be effectively handled by off-the-shelf solvers.

B. OC-SVC-based uncertainty set

We leverage a popular learning-based anomaly detection method, one-class support vector clustering (OC-SVC), to construct the appropriate uncertainty set U_t [32]. For convenience, we omit the subscript t in this section. The idea of OC-SVC is to find a minima sphere in high-dimension feature space as the boundary to separate normal and abnormal data, which can be expressed as

$$\min_{R,o,\omega} \quad R^2 + \frac{1}{N\epsilon} \sum_{n \in \mathcal{N}} \omega_n, \qquad (\mathbf{P-SVC})$$

s.t.
$$\|\boldsymbol{\psi}(\boldsymbol{\xi}^{(n)}) - \boldsymbol{o}\|^2 \le R^2 + \omega_n, \quad \forall n \in \mathcal{N},$$
 (21)

$$\omega_n \ge 0, \quad \forall n \in \mathcal{N}, \tag{22}$$

where R is the radius of the sphere; ϵ is a controllable parameter; $\psi(\cdot)$ is a mapping function from the original space to high-dimensional feature space; o is the center of the sphere; and ω_n is a slack variable. The second term in the objective function is the penalty for outliers. By introducing

 TABLE I

 CLASSIFICATION OF SAMPLES

 Dual variables of samples
 Positions
 Categories

Dual variables of samples	1 051110115	Categories
$\begin{array}{c} \alpha_n = 0\\ \beta_n = 1/(N\epsilon) \end{array}$	$\ \boldsymbol{\phi}(\boldsymbol{\xi}^{(n)}) - \boldsymbol{o}\ ^2 < R^2$	Interiors
$\begin{array}{l} 0 < \alpha_n < 1/(N\epsilon) \\ 0 < \beta_n < 1/(N\epsilon) \end{array}$	$\ \boldsymbol{\phi}(\boldsymbol{\xi}^{(n)}) - \boldsymbol{o}\ ^2 = R^2$	Boundaries
$\begin{array}{c} \alpha_n = 1/(N\epsilon) \\ \beta_n = 0 \end{array}$	$\ \boldsymbol{\phi}(\boldsymbol{\xi}^{(n)}) - \boldsymbol{o}\ ^2 > R^2$	Outliers

dual variables α and β for (21) and (22), the KKT conditions of **P-SVC** are

$$\mathbf{1}^{\mathsf{T}}\boldsymbol{\alpha} = 1, \quad \boldsymbol{o} = \sum_{n \in \mathcal{N}} \alpha_n \boldsymbol{\phi}(\boldsymbol{\xi}^{(n)}), \quad \boldsymbol{\alpha} + \boldsymbol{\beta} = \frac{1}{N\epsilon} \cdot \mathbf{1}, \quad (23)$$

$$\omega_n \beta_n = 0, \quad \forall n \in \mathcal{N}, \tag{24}$$

$$\alpha_n \left(R^2 + \omega_n - \| \boldsymbol{\phi}(\boldsymbol{\xi}^{(n)}) - \boldsymbol{o} \|^2 \right) = 0, \quad \forall n \in \mathcal{N},$$
 (25)

where (23) is obtained by setting the derivative of the Lagrangian function to zero, and (24) and (25) represent the complementary slackness. Based on the previous KKT conditions, we can recognize the interiors, boundaries, and outliers, as shown in Table I. We refer to the samples on the boundary as boundary support vectors, and regard outliers and boundary support vectors as support vectors. The sets of support vectors and boundary support vectors are defined based on Table I:

$$SV = \{ n | \alpha_n > 0, \ \forall n \in \mathcal{N} \},$$
(26)

$$BSV = \{n | 0 < \alpha_n < 1/(N\epsilon), \ \forall n \in \mathcal{N}\}.$$
 (27)

Note that the solutions of α and β can be obtained by solving the dual problem of **P-SVC**, as follows

$$\min_{\boldsymbol{\alpha}} \sum_{n \in \mathcal{N}} \sum_{m \in \mathcal{N}} \alpha_n \alpha_m K(\boldsymbol{\xi}^{(n)}, \boldsymbol{\xi}^{(m)}) - \sum_{n \in \mathcal{N}} K(\boldsymbol{\xi}^{(n)}, \boldsymbol{\xi}^{(m)}),$$
(D-SVC)

s.t.
$$0 \ge \alpha_n \ge \frac{1}{N\epsilon}, \forall n \in \mathcal{N},$$
 (28)

$$\sum_{n \in \mathcal{N}} \alpha_n = 1, \tag{29}$$

where $K(\boldsymbol{\xi}^{(n)}, \boldsymbol{\xi}^{(m)}) = \boldsymbol{\psi}(\boldsymbol{\xi}^{(n)})^{\mathsf{T}} \boldsymbol{\psi}(\boldsymbol{\xi}^{(m)})$ is the kernel function. This paper employs the weighted generalized intersection kernel [32] as our kernel function,

$$K(\boldsymbol{\xi}^{(1)}, \boldsymbol{\xi}^{(2)}) = \sum_{d \in \mathcal{D}} l_d - \| \boldsymbol{W}(\boldsymbol{\xi}^{(1)} - \boldsymbol{\xi}^{(2)}) \|_1, \qquad (30)$$

where $\mathcal{D} = \{1, 2, \dots, D\}$ is the dimension index set of $\boldsymbol{\xi}^{(1)}$ or $\boldsymbol{\xi}^{(2)}$; $l_d = \xi_{d,\max} - \xi_{d,\min}$, where $\xi_{d,\max}$ and $\xi_{d,\min}$ are the upper and lower bounds, respectively, of $\boldsymbol{\xi}$ in the *d*-th dimension; and $\boldsymbol{W} = \boldsymbol{\Sigma}^{-1/2}$, where $\boldsymbol{\Sigma}$ is the covariance matrix of the historical samples. Note that $K(\boldsymbol{\xi}, \boldsymbol{\xi}) = \sum_{d \in \mathcal{D}} l_d$ is a constant.

Proposition 1. The OC-SVC-based uncertainty set, i.e., $\mathcal{U} = \|\phi(\boldsymbol{\xi}^{(n)}) - \boldsymbol{o}\|^2 \leq R^2$, can be expressed as a polyhedron in the original space of uncertainty $\boldsymbol{\xi}$, as follows:

$$\mathcal{U} = \left\{ \boldsymbol{\xi} \left| \begin{array}{l} \exists \boldsymbol{v}_n \in \mathbb{R}^D, \forall n \in SV, \ s.t. \\ \sum_{n \in SV} \alpha_n \boldsymbol{v}_n^{\mathsf{T}} \mathbf{1} \leq \gamma, \\ -\boldsymbol{v}_n \leq \boldsymbol{W}(\boldsymbol{\xi} - \boldsymbol{\xi}^{(n)}) \leq \boldsymbol{v}_n, \forall n \in SV, \end{array} \right\}, \quad (31)$$

where \boldsymbol{v}_n is an auxiliary variable. Parameter γ is equal to $\sum_{n \in SV} \alpha_n \| \boldsymbol{W}(\boldsymbol{\xi}^{(k)} - \boldsymbol{\xi}^{(n)}) \|_1$ for any $k \in BSV$.

Proof: see Appendix A.

As mentioned above, a desirable uncertainty set must satisfy the feasibility, optimality, and tractability requirements. We show that the OC-SVC-based uncertainty set can meet the feasibility requirement.

Proposition 2. The uncertainty set U defined in (31) can cover at least $100(1 - \epsilon)\%$ of samples.

Proof: From Table I, we know that any outlier must have $\alpha_n = 1/(N\epsilon)$. If the number of outliers exceeds $N\epsilon$, then $\mathbf{1}^{\mathsf{T}} \boldsymbol{\alpha} > 1$ ($\alpha_n \ge 0$ for all samples), which conflicts with KKT condition (23). Hence the number of outliers must be no larger than $N\epsilon$, and the proposed uncertainty set can cover at least $100(1-\epsilon)\%$ of samples.

We verify the optimality performance of the proposed uncertainty set based on numerical experiments in section IV.

Since \mathcal{U} is a polyhedron, we can find a linear counterpart for it, as we next discuss. Hence the tractability requirement can also be satisfied. This tractability requirement is also the main reason for choosing the weighted generalized intersection as our kernel function. In fact, many other kernels, e.g., radial basis function, can also be applied to the OC-SVC [33]. However, they may lead to non-convex uncertainty sets. As a result, it is hard to find a tractable counterpart when other kernel functions are employed.

C. Linear robust counterpart

We develop a linear counterpart for the robust approximation (20) to make the whole problem tractable. First, based on (17), the robust approximation (20) can be expressed as

$$\max_{\boldsymbol{\xi}_{t} \in \mathcal{U}_{t}} \left\{ \max_{\forall m \in \mathcal{M}} \left((\boldsymbol{H}_{m,t} \boldsymbol{\xi}_{t})^{\mathsf{T}} \boldsymbol{y}_{t} - b_{m,t}(\boldsymbol{y}_{t}) \right) \right\} \leq 0,$$

$$\Leftrightarrow \max_{\boldsymbol{\xi}_{t} \in \mathcal{U}_{t}} \left((\boldsymbol{H}_{m,t} \boldsymbol{\xi}_{t})^{\mathsf{T}} \boldsymbol{y}_{t} \right) \leq b_{m,t}(\boldsymbol{y}_{t}), \forall m \in \mathcal{M}.$$
(32)

Based on the following proposition, we can find a linear counterpart for the robust constraint (32).

Proposition 3. If the uncertainty set is defined by (31), then (32) can be reformulated as linear constraints,

$$\begin{cases} \sum_{n \in SV_t} (\boldsymbol{\mu}_{n,m,t} - \boldsymbol{\rho}_{n,m,t})^{\mathsf{T}} \boldsymbol{W}_t \boldsymbol{\xi}_t^{(n)} + \pi_{m,t} \gamma_t \leq b_{m,t}, \\ \sum_{n \in SV_t} \boldsymbol{W}_t (\boldsymbol{\rho}_{n,m,t} - \boldsymbol{\mu}_{n,m,t}) + \boldsymbol{H}_{m,t}^{\mathsf{T}} \boldsymbol{y}_t = \boldsymbol{0}, \\ \boldsymbol{\rho}_{n,m,t} + \boldsymbol{\mu}_{n,m,t} = \pi_{m,t} \alpha_{n,t} \boldsymbol{1}, \quad \pi_{m,t} \geq 0, \\ \boldsymbol{\mu}_{n,m,t}, \boldsymbol{\rho}_{n,m,t} \in \mathbb{R}^D_+, \forall n \in SV_t, \forall m \in \mathcal{M}, \forall t \in \mathcal{T}, \end{cases}$$
(33)

where $\rho_{n,m,t}$, $\mu_{n,m,t}$, and $\pi_{m,t}$ are Lagrange multipliers for the m-th constraint at time t in (32).

Proof: see Appendix B.

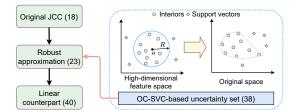


Fig. 1. The whole procedure for converting JCCs into linear constraints.

D. Summary

Based on the previous linear counterpart, we can reformulate problem **P1** as:

$$\min_{\boldsymbol{y}_t, \forall t \in \mathcal{T}} \sum_{t \in \mathcal{T}} \mathbb{E}\left(\sum_{t \in \mathcal{T}} EC_t\right), \quad (\mathbf{P2})$$
s.t. Eqs. (1)-(4), (5)-(11), (7)-(9), (14), and (33).

Fig. 1 summarizes the procedure to convert intractable JCCs to tractable linear constraints. We develop a robust optimizationbased approximation (20) for the original JCC (15), and solve the dual problem **D-SVC** to find the support vectors and construct the OC-SVC-based uncertainty set (31). We implement the linear counterpart based on (33) to replace the original intractable JCC, and solve problem **P2** to obtain the optimal schedule of HVAC systems and DRG.

Although this paper only involves the uncertainties from DRG, the proposed model can readily consider uncertainties from other sources. For example, if power demands are uncertain, then p_t^e and q_t^e in (7)-(8) need to be treated as new uncertain parameters. Nevertheless, the constraints inside the probability operator of the JCC (12) are still linear. As a result, we can directly use the proposed model to construct a linear counterpart for this JCC.

IV. CASE STUDY

A. Simulation set up

We describe a case study based on the IEEE 13-bus system with wind turbines DRG1 and DRG2 to provide DRG, as shown in Fig. 2(a). The network parameters (e.g., branch resistance and reactance) can be found on the IEEE website [34]. The indoor heat loads and base power demands (i.e., demands except HVAC loads) in different nodes are illustrated in Fig. 2(b)–(d). The unit prices for purchasing and selling electricity are shown in Fig. 3(a), and Fig. 3(b) shows the nominal outputs of DRG and outdoor temperature. The optimization horizon is set as 24h, and the time interval is one hour. Other parameters can be found in Table II. Because the forecasting errors of wind generation can be variant, we implement **Cases 1–3** with samples generated by Beta, Weibull, and Gaussian distributions, respectively, to simulate the historical data. The generated data has been uploaded on [35].

All numerical experiments are tested on an Intel 8700 3.20-GHz CPU with 16 GB memory. GUROBI and CVXPY are employed to solve the optimization problem.

B. Benchmarks

We introduce three models as benchmarks:

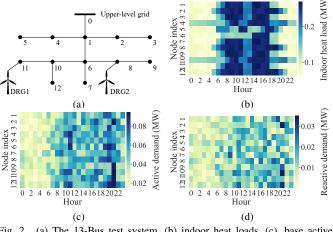


Fig. 2. (a) The 13-Bus test system, (b) indoor heat loads, (c), base active power demands, and (d) base reactive power demands. In (a), symbols "DRG1" and "DRG2" represent two distributed renewable generators.

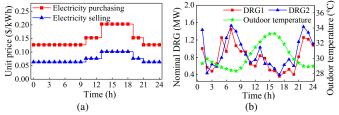


Fig. 3. (a) Unit prices of electricity purchasing and selling and (b) nominal outputs of DRG and outdoor temperature.

- B1(SA+Box): Scenario approach combined with a box uncertainty set [24], [25];
- B2(SA+CH): Scenario approach combined with a convex hull uncertainty set [27];
- 3) **B3(Bonferroni**): Bonferroni approximation, which approximates the original JCC with multiple ICCs [20].³

We also tested the performance of SAA. However, since it requires multiple constraints for every historical sample, the out-of-memory issue occurs, which implies a huge computational burden. Parameters used in simulations are consistent among all methods, so their results can be compared.

C. Computational cost of the learning step

The proposed model is based on a trained OC-SVC model, and the training process is implemented by scikit-learn, a famous machine-learning library for Python [36]. Fig. 4 summarizes the time spent on this learning step in different cases. Because OC-SVC is a mature machine learning model, it can be trained well in a short time. In all cases, the time spent on learning is less than 10s. Moreover, this learning step can be conducted offline because it requires no real-time demand information. Hence, it does not affect the computational efficiency of real-time scheduling.

D. Case 1: Beta distributed uncertainties

1) Shape of uncertainty sets: Fig. 5 illustrates the shapes of uncertainty sets constructed by different models based on

³The uncertainties in ICCs may not be normally distributed. In order to guarantee feasibility, we employ the moment-based distributionally robust chance constrained method used in [16] to reformulate these ICCs as second-order cone constraints.

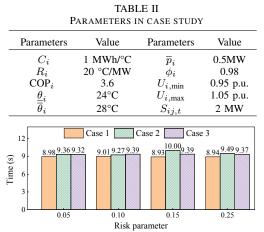


Fig. 4. Time spent on the learning step in different cases.

the samples at t = 6 in **Case 1**. Since the scenarios are randomly drawn, some extreme samples are chosen. Hence, the uncertainty sets of scenario approach-based models **B1** and **B2** must be large enough to cover these extreme samples, which is unnecessarily conservative. Unlike **B1** and **B2**, the proposed model introduces OC-SVC to decide which samples must be covered. By solving **P-SVC**, samples that are far from the majority of samples can be recognized as outliers. Compared to **B1** and **B2**, samples covered by the proposed uncertainty set are more concentrated, and the proposed uncertainty set (bounded by the green cross in Fig. 5) is much smaller. These results indicate that the proposed model can achieve better optimality than **B1** and **B2**.

2) Optimality, feasibility and time-efficiency: Fig. 6 summarizes the energy cost, average utilization rate of DRG, solution time, and maximum violation probability obtained by different models. The energy cost of Bonferroni approximation **B3** is the worst among all models because the number of constraints in the original JCC (15) is relatively large, and the risk parameter of each ICC is too small (less than 0.0015), leading to a conservative solution. The proposed model achieves the lowest energy cost and highest utilization

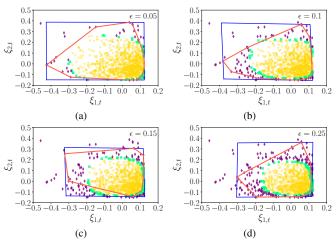


Fig. 5. Uncertainty sets in **Case 1** (uncertainties follow Beta distribution) generated by different models at t = 6: (a) $\epsilon = 0.05$; (b) $\epsilon = 0.10$; (c) $\epsilon = 0.15$; (d) $\epsilon = 0.25$. Blue rectangle and red polyhedron indicate uncertainty sets constructed by **B1(SA+Box)** and **B2(SA+CH)**, respectively. SVC-based uncertainty set is formed by boundary support vectors (green points). Internal samples and outliers are marked as gold dots and purple diamonds, respectively.

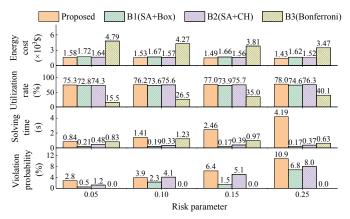


Fig. 6. Results of energy costs, average utilization rates of DRG, solving times, and maximum violation probabilities obtained by different models in **Case 1** (Uncertainties follow the Beta distribution).

rate of DRG. The proposed OC-SVC-based uncertainty set can cover the historical samples more tightly than conventional box and convex hull uncertainty sets. Hence the solution is less conservative (i.e., the energy cost is smaller), and more DRG can be utilized in distribution networks; e.g., the average utilization rate of DRG obtained by the proposed model is around 2.5% and 1.5% higher than in **B1** and **B2**, respectively. These results confirm that the proposed model can better promote DRG utilization.

The solving time of the proposed model is always larger than those of **B1-B3** because it needs to introduce more constraints. According to (33), the proposed model needs to introduce $|\mathcal{M}| \cdot |SV_t|$ constraints for each JCC. The value of $|\mathcal{M}| \cdot |SV_t|$ is relatively large, so the corresponding computational burden is high. Conversely, since our test system only contains two renewable generators, the dimension number of the uncertainty vector is low, resulting in a relatively small scenario number in **B1** and **B2** [24], [25]. Thus, a simple uncertainty set can cover all these scenarios, so the counterparts of **B1** and **B2** only contain a small number of constraints. **B3** approximates the original JCC into multiple ICCs, and the number of ICCs is equal to $|\mathcal{M}|$, which is much smaller than that in the proposed model. As a result, the computational efficiency of the proposed model is the worst. Nevertheless, the maximum solving time of the proposed model is only around 4s. Given that the optimization horizon is 24h, this computational efficiency is acceptable. Moreover, its solving time decreases with the risk parameter's decrease. Obviously, if the risk parameter is small, then only a few samples of uncertainties are allowed to violate constraints. In this case, the support vector number $|SV_t|$ is also small. As a result, only a few constraints are introduced, resulting in a lower computational burden. For example, when $\epsilon = 0.05$, it can complete the solution process in 1s. Considering that the risk parameter is commonly maintained at a low level, the proposed model can meet the computational efficiency requirements well in practice.

The violation probabilities of the original JCC (15) obtained by all models, including the proposed one, are always lower than the given risk parameter. For **B1–B3**, it has been pointed out [10] that they provide conservative approximations for

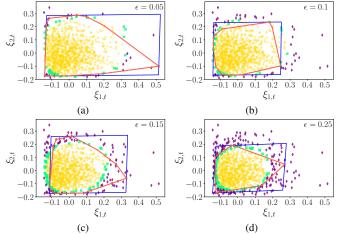


Fig. 7. Uncertainty sets generated by different models in **Case 2** (uncertainties follow Weibull distribution) at t = 6: (a) $\epsilon = 0.05$; (b) $\epsilon = 0.10$; (c) $\epsilon = 0.15$; (d) $\epsilon = 0.25$.

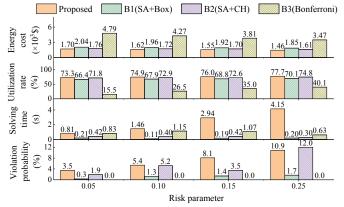


Fig. 8. Results of energy costs, average utilization rates of DRG, solution times, and maximum violation probabilities obtained by different models in **Case 2** (uncertainties follow Weibull distribution).

JCCs. Eqs. (18)–(20) imply that the proposed model is also an inner approximation. Hence all four models can guarantee feasible solutions.

E. Case 2: Weibull distributed uncertainties

1) Shape of uncertainty sets: Fig. 7 shows the uncertainty sets established by different models in **Case 2**. Similar to **Case 1**, the proposed OC-SVC-based method can capture the characteristics of the Weibull distribution and tightly cover most samples. Therefore, the unnecessary space introduced by the proposed uncertainty set is smaller than those of scenario approaches **B1** and **B2**.

2) Optimality, feasibility and time-efficiency: The results of different models in **Case 2** are listed in Fig. 8. Bonferroni approximation **B3** shows the worst energy efficiency because of the small risk parameter in each ICC. With the smallest volume of the OC-SVC-based uncertainty set, the proposed model achieves the highest energy efficiency and utilization rate of DRG with proper feasibility.

F. Case 3: Normally distributed uncertainties

1) Shape of uncertainty sets: Fig. 9 presents the results of uncertainty sets constructed by different models with normally distributed uncertainties. Similar to **Cases 1** and **2**, the

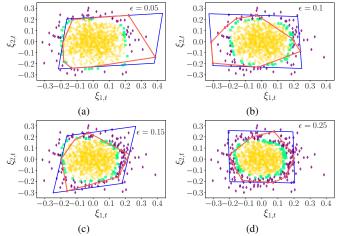


Fig. 9. Uncertainty sets generated by different models in **Case 3** (uncertainties follow a Gaussian distribution) at t = 6: (a) $\epsilon = 0.05$; (b) $\epsilon = 0.10$; (c) $\epsilon = 0.15$; (d) $\epsilon = 0.25$.

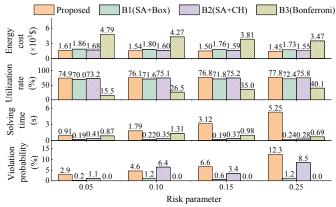


Fig. 10. Results of energy costs, average utilization rates of DRG, solution times, and maximum violation probabilities obtained by different models in **Case 3** (uncertainties follow a Gaussian distribution).

proposed uncertainty set has the smallest volume. The other two are relatively large because they must cover some extreme samples (such as at the bottom-right corner).

2) Optimality, feasibility and time-efficiency: Fig. 10 summarizes the energy cost, average utilization rate of DRG, solution time, and maximum violation probability. The energy cost of the proposed model is the lowest, e.g., 13.4%, 4.2%, and 66.4% less than those of **B1–B3**, respectively, with risk parameter $\epsilon = 0.05$. Its utilization rate of DRG is also the highest, e.g., 4.9%, 1.7%, and 59.4% higher than those of **B1–B3**, respectively, at $\epsilon = 0.05$. Although its solution time is greater, the computational efficiency is still acceptable.

The results in **Cases 1–3** also confirm that the proposed model can handle JCCs with arbitrarily distributed uncertainties, confirming its generalization performance.

G. Effectiveness under correlated uncertainties

In practice, the outputs of DRG in one distribution network may be correlated. This correlation shall be properly considered because it may significantly affect the decision of power scheduling [37]. In fact, this correlation can help to eliminate many unlikely-to-happen scenarios and improve the accuracy of uncertainty sets [38]. Since the proposed model constructs the uncertainty set based on historical samples, it can easily

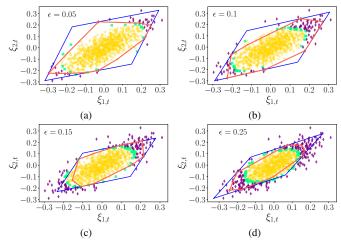


Fig. 11. Uncertainty sets generated by different models at t = 6 in the case with correlated uncertainties: (a) $\epsilon = 0.05$; (b) $\epsilon = 0.10$; (c) $\epsilon = 0.15$; (d) $\epsilon = 0.25$.

capture this correlation. As a result, the proposed model can also be applied to the cases with correlated uncertainties.

To better verify the effectiveness of the proposed model, we further implement a case with correlated uncertainties. Specifically, this case assumes that the uncertainties from the DRG1 and DRG2 in Fig. 2(a) follow a joint Gaussian distribution. The expectation μ and covariance **Cov** of this joint distribution are:

$$\boldsymbol{\mu} = (0,0), \quad \mathbf{Cov} = \begin{bmatrix} 0.01 & 0.008\\ 0.008 & 0.01 \end{bmatrix}.$$
 (34)

B1-B3 are also introduced as benchmarks for comparison.⁴

Fig. 11 illustrates the shapes of uncertainty sets constructed by different models based on the samples at t = 6 in the case with correlated uncertainties. Similar to **Cases 1-3**, the uncertainty sets of **B1** and **B2** must be large enough to cover these extreme samples. Conversely, the proposed uncertainty set can cover most samples more tightly, so it is the smallest one, which indicates its desirable optimality.

Fig. 12 summarizes the energy cost, average utilization rate of DRG, solution time, and maximum violation probability obtained by different models. **B3** always derives the highest energy cost and lowest utilization rate of distributed renewable generation (DRG) among all models because the risk parameter in each ICC is very small. The proposed model achieves the lowest energy cost and highest utilization rate of DRG because its uncertainty set is the smallest. Although its computational performance is worse than other models, the maximum solving time is only 2.93s, which is acceptable in practice. All four models, including the proposed one, can guarantee feasibility because all of them are based on inner approximations of the intractable JCC. These results confirm that the proposed model can achieve desirable optimality and feasibility with guaranteed computational efficiency.

H. Effectiveness under heterogeneous parameters

In Cases 1–3, we assume that the building parameters of all

⁴Since the uncertainties here are normally distributed, we use the widely used second-order cone reformulation for the chance constraints with Gaussian uncertainties to handle each ICC [10].

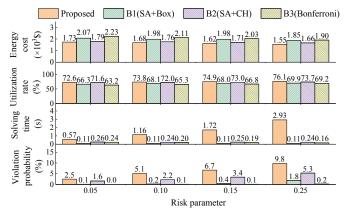


Fig. 12. Results of energy costs, average utilization rates of distributed renewable generation, solution times, and maximum violation probabilities obtained by different models in the case with correlated uncertainties.

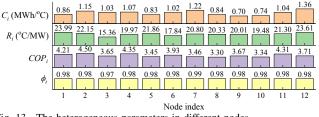


Fig. 13. The heterogeneous parameters in different nodes.

nodes are homogeneous. To better verify the performance of the proposed model, we implement a case study in which different nodes have heterogeneous parameters. Fig. 13 shows the heat capacity C_i of the building, thermal resistance R_i between indoor and outdoor environments, coefficient of performance COP_i , and coefficient $\sqrt{(1-\phi_i^2)}/\phi_i$ used in (3). Buildings connected to different nodes obviously have heterogeneous parameters and various demands.

Fig. 14 summarizes the results of this case study. Even with some heterogeneity in the parameters, the proposed model achieves the highest energy efficiency and utilization rate of DRG. Moreover, the violation probability of the JCC is always less than the given risk parameter. Although the solution time is longer, the maximum solution time is only 3.36 s.

I. Effectiveness of flexibility from HVAC loads

Fig. 15 shows the indoor temperatures, total heating load (heat loads from indoor sources plus heat transfer from outdoor

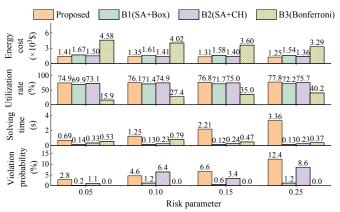


Fig. 14. Simulation results in the case with heterogeneous parameters.

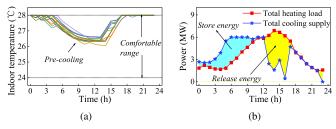


Fig. 15. Results of (a) indoor temperatures and (b) total heating load and cooling supply with Beta distributed uncertainties and $\epsilon = 0.05$.

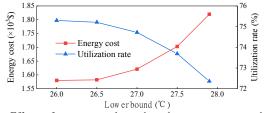


Fig. 16. Effects of temperature lower bound on energy cost and average utilization rate of DRG with $\epsilon = 0.05$.

environments), and cooling supply. The results are obtained by the proposed model with Beta distributed uncertainties with $\epsilon = 0.05$. During the period from 4:00 a.m. to 12:00 a.m., a significant temperature drop occurs in each building, which we refer to as pre-cooling, and the energy storage is based on this. During these hours, the available DRG power is relatively high, and the electricity price is low. To reduce the whole-day energy cost, the distribution network unlocks building thermal flexibility to store as much cooling power as possible for later use. Thus, the total cooling supply is much higher than the required total heating load during this period, as shown in Fig. 15(b). In the next few hours, the electricity price increases while the available DRG power decreases, and the stored cooling power is released. Therefore, the total cooling supply is visibly lower than the total heating load, leading to a noticeable increase in indoor temperatures. These results confirm that buildings can serve as batteries to provide operational flexibility for distribution networks.

Since the energy storage of buildings is based on precooling, the variation of the lower bound of the indoor temperature, i.e., $\underline{\theta}$, influences the capacity of the building's thermal flexibility. We change $\underline{\theta}$ to verify the effectiveness of this flexibility, with results as shown in Fig. 16. With the growth of $\underline{\theta}$, the capacity of the building thermal flexibility becomes smaller because less cooling power can be stored in indoor environments, leading to a lower utilization rate of DRG and higher energy cost.

V. CONCLUSIONS

This paper proposes a learning-based approach to promote DRG integration by scheduling flexible HVAC loads. The violation probabilities of all critical constraints are managed by JCCs to ensure the security of the whole system. To overcome the intractability of JCCs, this paper develops a robust constraint with a novel OC-SVC-based polyhedron uncertainty set to safely approximate JCCs. A linear counterpart was developed to guarantee computational efficiency. Numerical experiments on an IEEE 13-bus system indicated that the proposed uncertainty set can tightly cover most

APPENDIX A

Bonferroni approximation. Simulation results also confirm that

the flexibility of HVAC loads can promote the integration of

DRG and enhance energy efficiency.

Proof of Proposition 1: According to Table I, the radius R is equal to the distance from the vector o to any boundary support vector,

$$R^2 = \|\boldsymbol{\phi}(\boldsymbol{\xi}^{(k)}) - \boldsymbol{o}\|^2, \quad k \in \text{BSV}.$$
(35)

Based on (23), we can substitute $o = \sum_{n \in \mathcal{N}} \alpha_n \phi(\boldsymbol{\xi}^{(n)})$ in (35) to obtain

$$R^{2} = K(\boldsymbol{\xi}^{(k)}, \boldsymbol{\xi}^{(k)}) - 2 \sum_{n \in \mathcal{N}} \alpha_{n} K(\boldsymbol{\xi}^{(k)}, \boldsymbol{\xi}^{(n)}) + \sum_{n \in \mathcal{N}} \sum_{m \in \mathcal{N}} \alpha_{n} \alpha_{m} K(\boldsymbol{\xi}^{(n)}, \boldsymbol{\xi}^{(m)}), k \in \text{BSV}.$$
(36)

Similarly, by substituting $\boldsymbol{o} = \sum_{n \in \mathcal{N}} \alpha_n \boldsymbol{\phi}(\boldsymbol{\xi}^{(n)})$, the region bounded by the minima sphere, i.e., $\{\boldsymbol{\xi} \mid \|\boldsymbol{\phi}(\boldsymbol{\xi}) - \boldsymbol{o}\|^2 \leq R^2\}$, can be expressed as

$$\mathcal{U} = \left\{ \boldsymbol{\xi} \left| K(\boldsymbol{\xi}, \boldsymbol{\xi}) - 2 \sum_{n \in \mathcal{N}} \alpha_n K(\boldsymbol{\xi}, \boldsymbol{\xi}^{(n)}) + \sum_{n \in \mathcal{N}} \sum_{m \in \mathcal{N}} \alpha_n \alpha_m K(\boldsymbol{\xi}^{(n)}, \boldsymbol{\xi}^{(m)}) \le R^2 \right\}.$$
(37)

Then, substituting (36) and (30) in (37), we can rewrite the uncertainty set as

$$\mathcal{U} = \left\{ \boldsymbol{\xi} \left| \sum_{n \in \mathcal{N}} \alpha_n K(\boldsymbol{\xi}, \boldsymbol{\xi}^{(n)}) \geq \sum_{n \in \mathcal{N}} \alpha_n K(\boldsymbol{\xi}^{(k)}, \boldsymbol{\xi}^{(n)}) \right. \right\} \\ = \left\{ \boldsymbol{\xi} \left| \sum_{n \in SV} \alpha_n \| \boldsymbol{W}(\boldsymbol{\xi} - \boldsymbol{\xi}^{(n)}) \|_1 \leq \gamma \right\},$$
(38)

where $\gamma = \sum_{n \in SV} \alpha_n \| \boldsymbol{W}(\boldsymbol{\xi}^{(k)} - \boldsymbol{\xi}^{(n)}) \|_1$. By introducing auxiliary variable \boldsymbol{v}_n , the L1-norm operator can be eliminated, and \mathcal{U} can be reformulated as (31) in **Proposition** 1.

APPENDIX B

Proof of Proposition 3: The LHS term in (32) is equivalent to the following linear programming problem:

$$\max_{\boldsymbol{\xi}_{t}, \boldsymbol{\upsilon}_{n,t}} (\boldsymbol{H}_{m,t}\boldsymbol{\xi}_{t})^{\mathsf{T}}\boldsymbol{y}_{t},$$
(P-A1)
s.t. $\sum_{n \in \mathrm{SV}_{t}} \alpha_{n,t} \boldsymbol{\upsilon}_{n,t}^{\mathsf{T}} \mathbf{1} \leq \gamma_{t},$ $-\boldsymbol{\upsilon}_{n,t} \leq \boldsymbol{W}(\boldsymbol{\xi}_{t} - \boldsymbol{\xi}_{t}^{(n)}) \leq \boldsymbol{\upsilon}_{n,t}, \quad \forall n \in \mathrm{SV}_{t}.$

By introducing Lagrange multipliers $\rho_{n,t}$, $\mu_{n,t}$, and π_t , we can obtain its dual problem:

$$\min_{\substack{\boldsymbol{\mu}_{n,m,t},\\ \boldsymbol{\pi}_{m,t}}} \sum_{n \in \mathrm{SV}_t} (\boldsymbol{\mu}_{n,m,t} - \boldsymbol{\rho}_{n,m,t})^{\mathsf{T}} \boldsymbol{W}_t \boldsymbol{\xi}_t^{(n)} + \pi_{m,t} \gamma_t,$$
(D-A1)

s.t.
$$\sum_{n \in SV_t} W_t(\boldsymbol{\rho}_{n,m,t} - \boldsymbol{\mu}_{n,m,t}) + \boldsymbol{H}_{m,t}^{\mathsf{T}} \boldsymbol{y}_t = \boldsymbol{0},$$
$$\boldsymbol{\rho}_{n,m,t} + \boldsymbol{\mu}_{n,m,t} = \pi_{m,t} \alpha_{n,t} \boldsymbol{1},$$
$$\pi_{m,t} \ge 0, \quad \boldsymbol{\mu}_{n,m,t}, \boldsymbol{\rho}_{n,m,t} \in \mathbb{R}^D_+, \quad \forall n \in SV_t.$$

Note that **P-A1** is a linear problem, so the optimal solutions of **P-A1** and **D-A1** are equal based on strong duality. Finally, by substituting **D-A1** in (32), **Proposition** 3 can be proved.

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